### 11.8 Surface Area and Volume of Spheres

A sphere is the set of all points in space equidistant from a given point. This point is called the center of the sphere. A radius of a sphere is a segment from the center to a point on the sphere. A chord of a sphere is a segment whose endpoints are on the sphere. A diameter of a sphere is a chord that contains the center.


## Theorem 11.11 Surface Area of a Sphere

The surface area $S$ of a sphere is

$$
S=4 \pi r^{2},
$$

where $r$ is the radius of the sphere.


## Find the surface area of the sphere.

## Solution

$$
\begin{aligned}
S & =4 \pi r^{2} & & \text { Formula for surface area of a sphere } \\
& =4 \pi\left(8^{2}\right) & & \text { Substitute } 8 \text { for } r . \\
& =256 \pi & & \text { Simplify. } \\
& \approx 804.25 & & \text { Use a calculator. }
\end{aligned}
$$



The surface area of the sphere is about 804.25 square inches.

## Theorem 11.12 Volume of a Sphere

The volume $V$ of a sphere is

$$
V=\frac{4}{3} \pi r^{3},
$$

where $r$ is the radius of the sphere.
The soccer ball has a diameter of 9 inches. Find its volume.


## Solution

The diameter of the ball is 9 inches, so the radius is $\frac{9}{2}=4.5$ inches.

$$
\begin{aligned}
V & =\frac{4}{3} \pi r^{3} & & \text { Formula for volume of a sphere } \\
& =\frac{4}{3} \pi(4.5)^{3} & & \text { Substitute. } \\
& =121.5 \pi & & \text { Simplify. }
\end{aligned}
$$

